# Which Math Skills Are Students Missing? 

A Study of the Math Skill Gaps Most Prevalent Among Elementary and Middle School Students

## FOREWORD

Wouldn't it be great if all math students in a classroom came with the same experiences and same motivation to learn? It's a nice thought, but the reality is that there is a wide range of skills and readiness in every classroom. Teachers are faced with the challenge of making sure that every student is at grade level or above by the end of the school year. Combined with growing class sizes and changing standards and curriculum, this expectation for teachers today is overwhelming. The believed solution is to simply differentiate instruction. To do this well requires teachers to have a deep understanding of the curriculum, strong classroom management skills, and use assessment well.

Teachers also need to access the scope and sequence of skills before and after each particular grade level. Allowing students to grow in their academic endeavors as seen in academic gains should be the goal for all students regardless of where they start at the beginning of a unit of study. Integration of technology to support the learning as well as classroom management procedures, are critical for optimized student learning. Having a tool available to communicate any skill gaps helps teachers to better understand and plan strategically. Individualized instruction can be very difficult to manage, especially with a large class and a wide range of mathematically ability.

The use of web-based support materials in a blended learning environment can be an effective way to better fill in the missing skills and extend the learning of those working below and above grade level. Avon Intermediate School East has implemented Ascend Math for several years for the primary purpose of extending the learning for those students at or above grade level. Further analysis of recent statewide testing indicates that not only the amount of time spent using the program, but the leveling up and teacher intervention based on the reports are crucial to attain this growth. This was true for students who are below or on grade level as well.

We have found that Ascend Math has multiple uses, and it can be a very helpful tool to reduce skill gaps if implemented well. There are multiple reports and resources. Its flexibility is its greatest attribute.

Dr. Brian Scott, Principal of Avon Intermediate School East

## Introduction

What do students in need of math intervention have in common? Which skill gaps appear most frequently? Which are unique? Can students be effectively taught in small groups working on common objectives? When is individualized instruction warranted?

Since 2005, Ascend Education has gathered data on student math performance. For this study, 18,000 students identified for intervention were given a computer adaptive level placement test. This included students nationwide representing a wide diversity of demographics. The level placement test found each student's lowest functional level in math. At least $82 \%$ of these students had skill gaps below their current grade level. The study focused on these students.

Each student was provided a series of pre-assessments on objectives beginning at their functional grade level according to the level placement test. In this way, each student's individual math skill gaps were identified, captured and compiled for this report.

Data was examined for students from grades 2-8. However, only data for students in the fifth and seventh grades are included in this premiere version of the study. The data from more grades will be shared in future releases.

In-depth study continues, however, it would appear that this large case study conducted nationwide would strongly support the need for individualized instruction and study for each student identified for math intervention.

## About the Data



Grade 7 students in the study were widely dispersed. Only $5 \%$ had skill gaps just one grade below level. The remaining students were split almost evenly with their lowest skill gap from two to five grades below the seventh grade level.

## Results of Level Placement Test

Forty percent of grade 5 students in the study had skill gaps one grade below level. Another $28 \%$ had their lowest skill gap two grades below level. Nearly one third had their lowest skill gap three grades below the fifth grade level.


## Rankings

In this study, you will find the rankings of the most common skill gaps for these two grades within each level. For example, the first page is devoted to the $40 \%$ of fifth grade students with gaps one grade below level. Each page will be devoted to a single grade and functional grade level listing the most common skill gaps in that level. Although we chose to focus on the top 20-25, the list of skill gaps often runs much deeper. Complete listings will be provided in a future release.

## Study of Gaps in Scope and Sequence

Given that students are starting at different levels on different gaps it looks challenging at best for a teacher to make significant progress using small group instruction alone. To provide a better feel for this challenge each page also includes a listing of the objectives from that level in their proper scope and sequence. In this chart, you can easily observe the percentage of students still needing to master each objective in the level. In the interest of space, we chose to focus on the first 25 objectives for each grade level's sequence. Complete tables will be made available in a future release.

## Grade 5 Students

## Ranking of skill gaps for students placed at grade level 2

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Introduction to Addition | Even Numbers as a Sum of Equal Addends | 64\% |
| 2 | Introduction to Measurement | Picture and Bar Graph | 64\% |
| 3 | Introduction to Patterns | Introduction to Number Line Diagrams Using Whole Numbers | 62\% |
| 4 | Elementary Measurement | Modeling Time on a Number Line Diagram | 60\% |
| 5 | Introduction to Measurement | Foundations of Measurement | 56\% |
| 6 | Introduction to Money | Counting Money, Applications | 52\% |
| 7 | Introduction to Money | Making Change | 50\% |
| 8 | Introduction to Addition | Addition of Objects, Arrays and Equations | 41\% |
| 9 | Introduction to Odd and Even | Patterns with Numbers | 40\% |
| 10 | Introduction to Addition | Addition of Objects Using Arrays | 39\% |
| 11 | Introduction to Money | Counting Money, Review | 37\% |
| 12 | Introduction to Money | Money, Intro | 35\% |
| 13 | Elementary Subtraction | Vertical Subtraction, 2-Digit | 33\% |
| 14 | Elementary Subtraction | Vertical Subtraction, 3-Digit | 33\% |
| 15 | Introduction to Odd and Even | Skip Counting by 2s | 30\% |
| 16 | Introduction to Odd and Even | Skip Counting by 3s | 30\% |
| 17 | Introduction to Odd and Even | Odd and Even, Application | 29\% |
| 18 | Introduction to Money | Counting Money | 26\% |
| 19 | Introduction to Place Value | Place Value, Hundreds | 17\% |
| 20 | Elementary Addition | 2-Digit Addition, 3-Digit Answers | 9\% |
| 21 | Elementary Addition | 3-Digit Addition, 3-Digit Answers | 9\% |
| 22 | Elementary Addition | 2-Digit Addition, 2-Digit Answers | 0\% |
| 23 | Introduction to Odd and Even | Odd and Even | 0\% |



## Grade 5 Students

## Ranking of skill gaps for students placed at grade level 3

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Whole Number Addition and Subtraction | Properties of Addition with Whole Numbers | 88\% |
| 2 | Whole Numbers | Whole Numbers and Place Value | 83\% |
| 3 | Elementary Multiplication | The Concept of Perimeter and Area Models Connected to Addition | 77\% |
| 4 | Elementary Measurement | Measurement | 76\% |
| 5 | Whole Number Addition and Subtraction | Modeling Addition and Subtraction of Whole Numbers | 75\% |
| 6 | Whole Number Multiplication and Division | Properties of Multiplication with Whole Numbers | 73\% |
| 7 | Elementary Division | Understanding Division | 65\% |
| 8 | Whole Numbers | Greater Than \& Less Than | 54\% |
| 9 | Elementary Addition and Subtraction | 2\&3 Digit Subtraction | 50\% |
| 10 | Elementary Multiplication and Division with Two or More Digits | Modeling Multiplication and Division with Unknowns | 50\% |
| 11 | Elementary Measurement | Time | 50\% |
| 12 | Whole Number Multiplication and Division | Properties of Division | 50\% |
| 13 | Fractions Concepts | Understanding Unit Fractions Using Area Models | 50\% |
| 14 | Elementary Multiplication and Division with Two or More Digits | Multiplication and Division using Associative and Distributive Properties | 45\% |
| 15 | Whole Number Multiplication and Division | Multiplying Whole Numbers | 44\% |
| 16 | Elementary Multiplication | Interpreting Products of Whole Numbers Using Multiples of 10 | 43\% |
| 17 | Elementary Multiplication | Understanding Multiplication | 43\% |
| 18 | Elementary Division | Foundations of Division | 40\% |
| 19 | Elementary Multiplication and Division with Two or More Digits | Relationship Between Multiplication and Division with Unknown-Factors | 40\% |
| 20 | Elementary Multiplication | Conceptual Multiplication Applications | 38\% |



## Grade 5 Students

## Ranking of skill gaps for students placed at grade level 4

## 40\%

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Whole Number Multiplication and Division | Guess and Check | 83\% |
| 2 | Fractions Concepts | Comparing Fractions Using Area Models | 76\% |
| 3 | Fractions Operations | Adding \& Subtracting Fractions | 75\% |
| 4 | Elementary Multiplication and Division with Two or More Digits | Multiplication and Division with Unknown Factors | 74\% |
| 5 | Whole Number Multiplication and Division | Mental Math | 69\% |
| 6 | Fractions Operations | Multiplying a Fraction by a Whole Number Using Area Models | 69\% |
| 7 | Fractions Concepts | Line Plots to Display Fractional Data | 67\% |
| 8 | Whole Number Addition and Subtraction | Associative and Commutative Properties | 67\% |
| 9 | Metric and Customary Systems of Measurement | Length, Capacity and Weight | 67\% |
| 10 | Geometry Concepts | Symmetry | 67\% |
| 11 | Whole Number Multiplication and Division | Modeling Multiplication of Whole Numbers | 64\% |
| 12 | Whole Number Multiplication and Division | Division with Remainders | 60\% |
| 13 | Fractions Operations | Modeling Addition and Subtraction of Fractions | 59\% |
| 14 | Geometry Concepts | Angles and Triangles | 57\% |
| 15 | Elementary Division | Foundations of Division Using Area Models | 54\% |
| 16 | Whole Number Factors and Multiples | Factor Pairs | 51\% |
| 17 | Elementary Multiplication | Foundation of Multiplication Using Place Value | 51\% |
| 18 | Whole Number Multiplication and Division | Distributive Property, Using Place Value Strategies | 50\% |
| 19 | Decimals Operations | Understanding Decimals | 50\% |
| 20 | Decimals Operations | Comparing Decimals to Hundredths | 50\% |



## Grade 7 Students

## Ranking of skill gaps for students placed at grade level 2

| Rank | Unit | Objective | \% |
| :---: | :--- | :--- | :---: |
| 1 | Introduction to Patterns | Introduction to Number Line Diagrams Using Whole Numbers | $78 \%$ |
| 2 | Elementary Measurement | Modeling Time on a Number Line Diagram | $78 \%$ |
| 3 | Introduction to Money | Making Change | $42 \%$ |
| 4 | Introduction to Addition | Even Numbers as a Sum of Equal Addends | $41 \%$ |
| 5 | Introduction to Measurement | Picture and Bar Graph | $39 \%$ |
| 6 | Introduction to Money | Counting Money, Applications | $35 \%$ |
| 7 | Introduction to Addition | Addition of Objects, Arrays and Equations | $33 \%$ |
| 8 | Introduction to Odd and Even | Odd and Even, Application | $33 \%$ |
| 9 | Introduction to Money | Counting Money, Review | $30 \%$ |
| 10 | Introduction to Odd and Even | Skip Counting by 3s | $29 \%$ |
| 11 | Introduction to Money | Counting Money | $27 \%$ |
| 12 | Elementary Subtraction | Vertical Subtraction, 3-Digit | $25 \%$ |
| 13 | Introduction to Place Value | Place Value, Hundreds | $20 \%$ |
| 14 | Elementary Subtraction | Vertical Subtraction, 2-Digit | $17 \%$ |
| 15 | Introduction to Addition | Addition of Objects Using Arrays | $14 \%$ |
| 16 | Elementary Addition | 2-Digit Addition, 2-Digit Answers | $11 \%$ |
| 17 | Introduction to Odd and Even | Patterns with Numbers | $11 \%$ |
| 18 | Introduction to Money | Money, Intro | $3 \%$ |
| 19 | Elementary Addition | 2-Digit Addition, 3-Digit Answers | $0 \%$ |
| 20 | Elementary Addition | 3-Digit Addition, 3-Digit Answers | $0 \%$ |
| 21 | Introduction to Odd and Even | Odd and Even | $0 \%$ |
| 22 | Introduction to Odd and Even | Skip Counting by 2s | $0 \%$ |
| 23 | Geometry Concepts | Understanding Shapes and their Attributes | $0 \%$ |



## Grade 7 Students

## Ranking of skill gaps for students placed at grade level 3

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Whole Numbers | Whole Numbers and Place Value | 86\% |
| 2 | Elementary Measurement | Measurement | 80\% |
| 3 | Elementary Multiplication | The Concept of Perimeter and Area Models Connected to Addition | 79\% |
| 4 | Elementary Multiplication | Applications of Multiplication Using Area Models | 72\% |
| 5 | Whole Numbers | Greater Than \& Less Than | 72\% |
| 6 | Whole Number Addition and Subtraction | Properties of Addition with Whole Numbers | 67\% |
| 7 | Fractions Concepts | Understanding Fractions | 60\% |
| 8 | Elementary Division | Understanding Division | 58\% |
| 9 | Elementary Multiplication | Interpreting Products of Whole Numbers Using Multiples of 10 | 57\% |
| 10 | Elementary Multiplication and Division with Two or More Digits | Modeling Multiplication and Division with Unknowns | 57\% |
| 11 | Elementary Measurement | Time | 57\% |
| 12 | Whole Number Addition and Subtraction | Modeling Addition and Subtraction of Whole Numbers | 57\% |
| 13 | Elementary Division | Foundations of Division | 56\% |
| 14 | Whole Number Multiplication and Division | Properties of Multiplication with Whole Numbers | 54\% |
| 15 | Elementary Multiplication and Division with Two or More Digits | Finding 2 Digit Quotients | 54\% |
| 16 | Whole Number Multiplication and Division | Multiplying Whole Numbers | 50\% |
| 17 | Whole Number Multiplication and Division | Properties of Division | 50\% |
| 18 | Fractions Concepts | Understanding Unit Fractions Using Area Models | 50\% |
| 19 | Statistics | Introduction to Bar Graphs | 50\% |
| 20 | Elementary Multiplication and Division with Two or More Digits | Relationship Between Multiplication and Division with Unknown-Factors | 45\% |



## Grade 7 Students

## Ranking of skill gaps for students placed at grade level 4

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Fractions Concepts | Comparing Fractions Using Area Models | 86\% |
| 2 | Fractions Operations | Adding \& Subtracting Fractions | 82\% |
| 3 | Fractions Operations | Multiplying a Fraction by a Whole Number Using Area Models | 79\% |
| 4 | Fractions Operations | Modeling Addition and Subtraction of Fractions | 77\% |
| 5 | Fractions Concepts | Line Plots to Display Fractional Data | 76\% |
| 6 | Elementary Multiplication and Division with Two or More Digits | Multiplication and Division with Unknown Factors | 74\% |
| 7 | Whole Number Multiplication and Division | Mental Math | 69\% |
| 8 | Whole Number Factors and Multiples | Factor Pairs | 69\% |
| 9 | Geometry Concepts | Symmetry | 69\% |
| 10 | Whole Numbers | Rounding Whole Numbers | 68\% |
| 11 | Metric and Customary Systems of Measurement | Length, Capacity and Weight | 66\% |
| 12 | Decimals Operations | Understanding Decimals | 63\% |
| 13 | Fractions Concepts | Understanding Unit Fractions on a Number Line Diagram | 56\% |
| 14 | Whole Number Multiplication and Division | Modeling Multiplication of Whole Numbers | 56\% |
| 15 | Geometry Concepts | Introduction to Symmetry | 55\% |
| 16 | Geometry Concepts | Angles and Triangles | 55\% |
| 17 | Elementary Division | Foundations of Division Using Area Models | 50\% |
| 18 | Whole Number Multiplication and Division | Guess and Check | 50\% |
| 19 | Geometry Concepts | Shapes and Their Attributes | 50\% |
| 20 | Geometry Concepts | Geometry Terms: Angles and Lines | 48\% |



## Grade 7 Students

## Ranking of skill gaps for students placed at grade level 5

\section*{24\%

## 24\%

## 24\%

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Whole Number Multiplication and Division | Modeling Division of Whole Numbers | 84\% |
| 2 | Fractions Concepts | Interpret a Fraction as Division of the Numerator by the Denominator | 75\% |
| 3 | Whole Number Multiplication and Division | Interpreting Multiplication as Scaling | 74\% |
| 4 | Fractions Operations | Multiplication, Using Area Models with Fractional Sides | 74\% |
| 5 | Whole Number Exponents and Order of Operations | Exponents and Place Value | 69\% |
| 6 | Whole Number Multiplication and Division | Order of Operations: Parentheses, Brackets, and Braces | 69\% |
| 7 | Fractions Operations | Modeling Whole Numbers Divided by Unit Fractions | 68\% |
| 8 | Metric and Customary Systems of Measurement | Converting Metric Measurements | 67\% |
| 9 | Fractions Operations | Multiplying a Fraction by a Whole Number Using Area Models | 64\% |
| 10 | Fractions Operations | Adding and Subtracting Fractions with Unlike Denominators | 58\% |
| 11 | Fractions Concepts | Finding Equivalent Fractions | 58\% |
| 12 | Fractions Applications | Modeling Addition and Subtraction of Fractions I | 55\% |
| 13 | Fractions Operations | Multiplying Fractions by Fractions | 54\% |
| 14 | Fractions Concepts | Comparing Fractions | 54\% |
| 15 | Decimals Operations | Dividing Decimals by Decimals | 53\% |
| 16 | Geometry Concepts | Parallelograms | 50\% |
| 17 | Fractions Concepts | Mixed Numbers and Their Equivalent Fractions | 46\% |
| 18 | Metric and Customary Systems of Measurement | Converting the Standard Measurements of Capacity and Mass | 46\% |
| 19 | Fractions Concepts | Introduction to Fractions | 46\% |
| 20 | Fractions Operations | Adding and Subtracting Fractions with Like Denominators | 45\% |



## Grade 7 Students

## Placed at Grade Level 6

| Rank | Unit | Objective | \% |
| :---: | :---: | :---: | :---: |
| 1 | Fractions Applications | Modeling Multiplication and Division of Fractions | 83\% |
| 2 | Fractions Applications | Modeling Perimeter and Area Using Whole Numbers and Fractions | 83\% |
| 3 | Integers and Real Numbers Concepts | Comparing Numbers in the Real World on a Number Line | 75\% |
| 4 | Fractions Applications | Modeling Division of Fractions in Story Context | 73\% |
| 5 | Fractions Applications | Modeling Multiplication of Fractions in Story Context | 73\% |
| 6 | Ratio and Proportion | Ratios Using Fraction Notation | 72\% |
| 7 | Whole Number Factors and Multiples | Least Common Multiple | 71\% |
| 8 | Fractions Operations | Multiplying and Dividing Mixed Numbers | 70\% |
| 9 | Metric and Customary Systems of Measurement | Converting the Standard Measurements of Length | 67\% |
| 10 | Metric and Customary Systems of Measurement | Converting the Standard Measurements of Capacity and Mass | 67\% |
| 11 | Metric and Customary Systems of Measurement | Converting Units of Mass | 67\% |
| 12 | Fractions Applications | Modeling Addition, Subtraction, Multiplication, and Division of Fraction | 63\% |
| 13 | Ratio and Proportion | Rates and Units Using Fraction Notation | 57\% |
| 14 | Metric and Customary Systems of Measurement | Converting Units of Capacity | 57\% |
| 15 | Decimals Operations | Multiplying Decimals | 54\% |
| 16 | Geometry Concepts | Solids | 53\% |
| 17 | Fractions Operations | Visualizing Quotients of Fractions | 52\% |
| 18 | Fractions Operations | Dividing Fractions by Fractions | 51\% |
| 19 | Decimals Operations | Converting Decimals to Fractions | 50\% |
| 20 | Geometry Concepts | Polygons in the Coordinate Plane | 50\% |

Objectives in Sequence Showing Student \% with Gap


## Individualized Instruction Begins at the Student's Lowest Skill Gap

As this report clearly shows, students identified for intervention have very different sets of skill gaps. Most math intervention programs offer only on-grade level instruction. For a math intervention program to be most effective it should include assessment that provides an individualized study plan for each student focused on their individual skill gaps plus instruction that allows students to move through their individual skill gaps at their own pace.

Ascend Math is intensive math intervention that meets each student at their lowest skill gap and guides each though an individualized study plan unique to each student. In this way, students with gaps three, four or more grades below level get the help they need.

Students learn best when they are engaged. That's why every instructional video and online exploration in Ascend is made interactive.

Students working just 1.5 to 2 hours a week in Ascend Math make tremendous progress, often gaining one to two grade levels in a semester or less. This happens because they are focused only on their individual needs.

Learn more at www.ascendmath.com or call toll-free (877) 843-0277.

## 7 Things to Consider When Choosing An Effective Math Intervention Program

|  |  | Ascend | Other |
| :---: | :---: | :---: | :---: |
| 1 | Intensive online math intervention that begins at the student's functional grade level. Students can progress through multiple levels on a single subscription. |  | $\bigcirc$ |
| 2 | Universal screener identifies skill gaps according to each state's rigorous standards. |  | $\bigcirc$ |
| 3 | Automatically assigns a unique study path at each level in which the student has skill gaps. |  | $\bigcirc$ |
| 4 | Real time data to make progress monitoring easy and give teachers a perspective on what each student needs and will receive next. |  | $\bigcirc$ |
| 5 | Gold standard multi-modal online instruction for more than 700 lessons/objectives. |  | $\bigcirc$ |
| 6 | Helps students gain a conceptual understanding of math standards through lessons and activities and provides students a methodology to write and speak about math. |  | $\bigcirc$ |
| 7 | Follows precisely the Standards for Mathematical Practice. |  | $\bigcirc$ |

